

TITLE

METHOD AND APPARATUS FOR I/Q IMBALANCE ESTIMATION

BACKGROUND OF THE INVENTION

Field of the Invention:

5 The present invention relates to signal estimation and compensation, and particularly to a method and apparatus for I/Q imbalance compensation and estimation.

Description of the Prior Art:

10 In a quadrature modulation/demodulation system, the real and imaginary parts of a baseband time-domain complex signal are transmitted simultaneously from the transmitter. They are carried on two orthogonal carriers (sine and cosine waves), respectively. The receiver uses the same orthogonal carriers to demodulate the received signal and derives the
15 original real and imaginary part of the baseband complex signal. The modulation/demodulation of the real part of the baseband complex signal is called in-phase (I) modulation/demodulation while that of the imaginary part is called quadrature-phase (Q) modulation/demodulation.

20 In practice, there is always a mismatch between I and Q modulation/demodulation, that is to say, there are always gain and phase offset in the I/Q modulated (or demodulated) signals. This is the I/Q imbalance known in the art.

25 FIG. 1A and 1B are diagrams respectively showing the I/Q imbalance at the receiver and transmitter. As shown in the figures, crosstalk occurs due to I/Q imbalance, which can not be eliminated even with the ACG (automatic gain

control) and carrier recovery circuitry. Further, ICI(inter carrier interference) also occurs for OFDM signals.

Conventionally, the solution to the previous problem is a circuitry system carefully designed to alleviate the I/Q imbalance. However, in an OFDM system, ICI is easily caused by I/Q imbalance because multi-carriers are used for high-speed transmission. This raises a need for a correction circuitry system, such as an equalizer or ICI eliminator. Even worse, in an OFDM system used for wireless LAN using burst mode transmission, the equalizer or ICI eliminator cannot achieve adequate compensation of I/Q imbalance.

SUMMARY OF THE INVENTION

The present invention provides a method for receiver I/Q imbalance estimation comprising the steps of transmitting a first OFDM signal by a first and second modulated carrier through a same modulation path at a transmitter, receiving the first OFDM signal by a first and second demodulated carrier respectively through a first and second demodulation path at a receiver, transmitting a second OFDM signal by the first and second modulated carrier through the same modulation path at the transmitter, receiving the second OFDM signal by the first and second demodulated carrier respectively through the first and second demodulation path at the receiver, and deriving an I/Q imbalance of the receiver by the first and second OFDM signal, wherein the first and second OFDM signal are symmetrical in frequency domain.

BRIEF DESCRIPTION OF THE DRAWINGS

The present invention will become more fully understood from the detailed description given hereinbelow and the accompanying drawings, given by way of illustration only and
5 thus not intended to be limitative of the present invention.

FIG. 1A and 1B are diagrams respectively showing the I/Q imbalance at the receiver and transmitter.

FIG. 2 is a diagram showing an apparatus for estimation and compensation of I/Q imbalance according to one
10 embodiment of the invention.

FIG. 3 is a diagram showing an estimator used in the apparatus for estimation and compensation of I/Q imbalance according to one embodiment of the invention.

FIG. 4A and 4B respectively show constellations of an
15 imbalanced modulation before and after the compensation.

DETAILED DESCRIPTION OF THE INVENTION

In the following embodiment of the invention, since there is usually no rapid variation in I/Q imbalance, the imbalance is estimated and corrected based upon the
20 characters of the OFDM transmitter or receiver when the system being started or idled.

As shown in FIG. 1A, the I/Q imbalance at the receiver is expressed as a 2×2 matrix function composed of parameters $\alpha_r \cos \theta_r$, $\alpha_r \sin \theta_r$, $\beta_r \cos \phi_r$ and $\beta_r \sin \phi_r$, where α_r and β_r are
25 gain offsets while θ_r and ϕ_r are phase offsets of the I and Q demodulation path in the receiver. The four parameters of the receiver I/Q imbalance matrix can be estimated by generating a signal with a specific frequency before inverse fast Fourier Transform (IFFT). The signal with the specific

frequency is transmitted in the form of a time-domain signal with either imaginary or real part power. Thus, the signal is transmitted through only one of the I and Q modulation paths of the transmitter. The gain and phase offsets of the signal can be compensated by the automatic gain control and carrier recovery circuit in the receiver. In this manner, the parameters $\alpha_r \cos \theta_r$ and $\beta_r \sin \theta_r$ are derived through transmitting a time-domain real part power signal while the parameters $\alpha_r \sin \theta_r$ and $\beta_r \cos \theta_r$ are derived through transmitting from a time-domain imaginary part power signal.

As shown in FIG. 1B, the I/Q imbalance at the transmitter is expressed as a 2*2 matrix function composed of parameters $\alpha_t \cos \theta_t$, $\alpha_t \sin \theta_t$, $\beta_t \cos \phi_t$ and $\beta_t \sin \phi_t$, where α_t and β_t are gain offsets while θ_t and ϕ_t are phase offsets of the I and Q modulation path in the transmitter. The four parameters of the transmitter I/Q imbalance matrix can be estimated by transmitting two signals, each of which includes the power of the real and imaginary part in time domain, in two different periods and demodulating them at the receiver through the same demodulation path. In the demodulation of each signal received by the receiver, two orthogonal carriers are used to respectively demodulate the real and imaginary parts of time-domain signals from the received signal. The parameters $\alpha_t \cos \theta_t$ and $\beta_t \sin \theta_t$ are derived from the real part of two receiving signals while the parameters $\alpha_r \sin \theta_r$ and $\beta_r \cos \theta_r$ are derived from the imaginary part of two receiving signals. The estimated signal may include the gain and phase offsets. However, it can be compensated by channel effect processing.

Accordingly, the I/Q imbalance estimation is based on transmitting/receiving signal through one single modulation/demodulation path to estimate the I/Q imbalance parameters. The baseband signal for the imbalance
5 estimation should be properly selected to simplify the estimation process.

FIG. 2 is a diagram showing an apparatus for estimation and compensation of I/Q imbalance according to one embodiment of the invention. The frequency-domain signal
10 generator 400 transmits a signal to the IFFT processor 550 converting the signal from frequency domain to time domain. The time-domain signal is sent to the transmitting compensating matrix circuit 250. The I modulation path of the transmitter includes a multiplexer MUX1, a D/A converter
15 200, a low-pass filter 22, and a mixer MIX1. The Q modulation path of the transmitter includes multiplexers MUX2, MUX3, MUX4, and MUX5, a D/A converter 202, low-pass filter 24, and mixer MIX2. The multiplexer MUX1 switch signals in the I modulation path while the multiplexers MUX2
20 and MUX3 switches signals in the Q modulation path. The multiplexers MUX4 and MUX5 select carriers for the I and Q modulation paths.

The I demodulation path of the receiver includes a mixer MIX3, a low-pass filter 21, an A/D converter 100 and a
25 multiplexer MUX6. The Q demodulation path of the receiver includes a mixer MIX4, a low-pass filter 23, an A/D converter 102, and multiplexers MUX 7 and MUX8. The signals going through the I and Q demodulation paths are sent to the receiving compensating matrix circuit 150 and then processed
30 by the AGC circuit 352 and carrier recovery circuit 350.

The FFT processor 500 converts the signal from the carrier recovery circuit 350 to a frequency-domain signal. The estimator 300 generates the parameters for the transmitting/receiving compensating matrix circuits 150 and 250. The multiplexer MUX6 switches signals in the I demodulation path while the multiplexers MUX7 and MUX8 select carriers for the I and Q demodulation paths.

The A/D converters 100 and 102 are followed by the receiving compensating matrix circuit 150 for compensation of the I/Q imbalance. Similarly, the D/A converters 200 and 202 are preceded by the transmitting compensating matrix circuit 250 for the same reason.

As shown in FIG. 1A, the receiver I/Q imbalance is expressed as:

$$\begin{bmatrix} y_i(t) \\ y_q(t) \end{bmatrix} = \begin{bmatrix} \alpha_r \cos \theta_r & \alpha_r \sin \theta_r \\ -\beta_r \sin \phi_r & \beta_r \cos \phi_r \end{bmatrix} \cdot \begin{bmatrix} x_i(t) \\ x_q(t) \end{bmatrix} \quad (1)$$

Thus, by deriving the four parameters $\alpha_r \cos \theta_r$, $\alpha_r \sin \theta_r$, $\beta_r \cos \phi_r$ and $\beta_r \sin \phi_r$, the compensation done by the receiving compensating matrix circuit 150 turns to be a matrix function:

$$\begin{bmatrix} \beta_r \cos \phi_r & -\alpha_r \sin \theta_r \\ \beta_r \sin \phi_r & \alpha_r \cos \theta_r \end{bmatrix} \quad (2)$$

The received signal is then expressed as:

$$\begin{bmatrix} r_i(t) \\ r_q(t) \end{bmatrix} = \begin{bmatrix} \beta_r \cos \phi_r & -\alpha_r \sin \theta_r \\ \beta_r \sin \phi_r & \alpha_r \cos \theta_r \end{bmatrix} \cdot \begin{bmatrix} y_i(t) \\ y_q(t) \end{bmatrix} \quad (3)$$

$$\begin{aligned} &= \begin{bmatrix} \beta_r \cos \phi_r & -\alpha_r \sin \theta_r \\ \beta_r \sin \phi_r & \alpha_r \cos \theta_r \end{bmatrix} \cdot \begin{bmatrix} \alpha_r \cos \theta_r & \alpha_r \sin \theta_r \\ -\beta_r \sin \phi_r & \beta_r \cos \phi_r \end{bmatrix} \cdot \begin{bmatrix} x_i(t) \\ x_q(t) \end{bmatrix} \\ &= [\alpha_r \cdot \beta_r \cdot \cos(\theta_r - \phi_r)] \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x_i(t) \\ x_q(t) \end{bmatrix} \quad (4) \end{aligned}$$

$[\alpha_r \cdot \beta_r \cdot \cos(\theta_r - \phi_r)]$ is the residual gain offset which is further compensated by the AGC circuit. The phase difference between the transmitted and received signal has no impact on the compensation since it is eliminated by the carrier recovery circuit.

Similarly, by deriving the four parameters $\alpha_t \cos \theta_t$, $\alpha_t \sin \theta_t$, $\beta_t \cos \phi_t$ and $\beta_t \sin \phi_t$, the compensation of the transmitter I/Q imbalance done by the transmitting compensating matrix circuit turns to be a matrix function:

$$\begin{bmatrix} \beta_t \cos \phi_t & \beta_t \sin \phi_t \\ -\alpha_t \sin \theta_t & \alpha_t \cos \theta_t \end{bmatrix} \dots \dots \dots (5)$$

The compensated signal is then expressed as:

$$\begin{bmatrix} y_i(t) \\ y_q(t) \end{bmatrix} = \begin{bmatrix} \alpha_t \cos \theta_t & -\beta_t \sin \phi_t \\ \alpha_t \sin \theta_t & \beta_t \cos \phi_t \end{bmatrix} \cdot \begin{bmatrix} v_i(t) \\ v_q(t) \end{bmatrix} \dots \dots \dots (6)$$

$$\begin{aligned} &= \begin{bmatrix} \alpha_t \cos \theta_t & -\beta_t \sin \phi_t \\ \alpha_t \sin \theta_t & \beta_t \cos \phi_t \end{bmatrix} \cdot \begin{bmatrix} \beta_t \cos \phi_t & \beta_t \sin \phi_t \\ -\alpha_t \sin \theta_t & \alpha_t \cos \theta_t \end{bmatrix} \cdot \begin{bmatrix} x_i(t) \\ x_q(t) \end{bmatrix} \\ &= [\alpha_t \cdot \beta_t \cdot \cos(\theta_t - \phi_t)] \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x_i(t) \\ x_q(t) \end{bmatrix} \dots \dots \dots (7) \end{aligned}$$

These parameters can be identified by correlation of a predetermined OFDM signal with that after an imbalanced I/Q modulation/demodulation.

When a signal x ($x_i + jx_q$) is converted to a signal y ($y_i + jy_q$) by a function:

$$\begin{bmatrix} y_i \\ y_q \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \cdot \begin{bmatrix} x_i \\ x_q \end{bmatrix} \dots \dots \dots (8),$$

the signal y is a linear combination of x and x^* , and can be expressed as:

$$y = C \cdot x + D \cdot x^* \dots \dots \dots (9)$$

where $C=c_i+jc_q$, $D=d_i+jd_q$, $c_i+d_i=A_{11}$, $-c_q+d_q=A_{12}$, $c_q+d_q=A_{21}$ and $c_i-d_i=A_{22}$.

If the signal $x(t)$ is a complex OFDM signal, then

$$x(t) = \sum_{k=-\frac{N}{2}}^{\frac{N}{2}} a_k \cdot e^{j2\pi f_s t} \dots\dots\dots (10)$$

$$y(t) = \sum_{k=-\frac{N}{2}}^{\frac{N}{2}} (C \cdot a_k + D \cdot a_{-k}) \cdot e^{j2\pi f_s t} \dots\dots\dots (11)$$

$$= \sum_{k=-\frac{N}{2}}^{\frac{N}{2}} \hat{a}_k \cdot e^{j2\pi f_s t} \dots\dots\dots (12)$$

where \hat{a}_k can be expressed by the following matrix form:

$$\begin{bmatrix} \hat{a}_{k,i} \\ \hat{a}_{k,q} \end{bmatrix} = \begin{bmatrix} c_i & -c_q \\ c_q & c_i \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} + \begin{bmatrix} d_i & d_q \\ d_q & -d_i \end{bmatrix} \cdot \begin{bmatrix} a_{-k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (13),$$

where a_k is the frequency-domain signal in k^{th} sub-channel,

10 $a_{k,i}$ is the real part of a_k and $a_{k,q}$ is the imaginary part of a_k .

Thus, the parameters used for compensating the I/Q imbalance can be derived by the equation (13) and characteristics of the OFDM signal. In order to avoid the impact of the transmitter I/Q imbalance, only one single demodulation path (either real-part modulation path I_{tx} or imaginary-part modulation path Q_{tx} of the transmitting node) is used during the estimation of the receiver I/Q imbalance.

20 When $a_{k,i} = a_{-k,i}$ (symmetric) and $a_{k,q} = -a_{-k,q}$ (anti-symmetric), only a real-part time-domain OFDM signal is transmitted. By transmitting this signal through only one

of the I and Q modulation paths (In this embodiment, the signal is transmitted through the Q modulation path and carried by a cosine ($\cos(\omega_c t)$) carrier wave) and demodulating the received signal by the FFT processor 500,

5 \hat{a}_k is:

$$\begin{aligned} \begin{bmatrix} \hat{a}_{k,i} \\ \hat{a}_{k,q} \end{bmatrix} &= \begin{bmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \\ &= \begin{bmatrix} c_i + d_i & -(c_q + d_q) \\ c_q + d_q & c_i + d_i \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (14) \end{aligned}$$

$$= \begin{bmatrix} \alpha_r \cos \theta_r & \beta_r \sin \phi_r \\ -\beta_r \sin \phi_r & \alpha_r \cos \theta_r \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (15)$$

When $a_{k,i} = -a_{-k,i}$ (symmetric) and $a_{k,q} = a_{-k,q}$ (symmetric),
10 only an imaginary-part time-domain OFDM signal is transmitted . By transmitting this signal through only one of the I and Q modulation paths (In this embodiment, the signal is transmitted through the I modulation path and carried by a sine ($-\sin(\omega_c t)$) carrier and demodulating the
15 received signal by the FFT processor 500, \hat{a}_k is turned to be:

$$\begin{bmatrix} \hat{a}_{k,i} \\ \hat{a}_{k,q} \end{bmatrix} = \begin{bmatrix} c_i - d_i & -(c_q - d_q) \\ c_q - d_q & c_i - d_i \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (16)$$

$$= \begin{bmatrix} \beta_r \cos \phi_r & \alpha_r \sin \theta_r \\ -\alpha_r \sin \theta_r & \beta_r \cos \phi_r \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (17)$$

Thus, from the equation (15), if $a_{k,i} = a_{k,q} = 1$, and $a_{-k,i} =$
20 $a_{k,i}$ and $a_{-k,q} = -a_{k,q}$, then

$$\begin{aligned} \hat{a}_{k,i} &= \alpha_r \cos \theta_r + \beta_r \sin \phi_r \dots\dots\dots (18) \\ \hat{a}_{k,q} &= -\beta_r \sin \phi_r + \alpha_r \cos \theta_r \end{aligned}$$

$$\begin{aligned}\alpha_r \cos \theta_r &= \frac{\hat{a}_{k,i} + \hat{a}_{k,q}}{2} \dots\dots\dots (19) \\ \beta_r \sin \phi_r &= \frac{\hat{a}_{k,i} - \hat{a}_{k,q}}{2}\end{aligned}$$

From the equation (17), if $a_{k,i}=a_{k,q}=1$, and $a_{-k,i}=-a_{k,i}$ and $a_{-k,q}=a_{k,q}$, then

$$\begin{aligned}\hat{a}_{k,i} &= \alpha_r \sin \theta_r + \beta_r \cos \phi_r \dots\dots\dots (20) \\ \hat{a}_{k,q} &= -\beta_r \cos \phi_r - \alpha_r \sin \theta_r\end{aligned}$$

$$\begin{aligned}\alpha_r \sin \theta_r &= \frac{\hat{a}_{k,i} - \hat{a}_{k,q}}{2} \dots\dots\dots (21) \\ \beta_r \cos \phi_r &= \frac{\hat{a}_{k,i} + \hat{a}_{k,q}}{2}\end{aligned}$$

Alternatively, the parameters $\alpha_r \cos \theta_r$, $\alpha_r \sin \theta_r$, $\beta_r \cos \phi_r$ and $\beta_r \sin \phi_r$ for the receiver I/Q imbalance compensation may also be estimated by correlation of predetermined and independent frequency-domain signals wherein $a_{k,i}=a_{k,q}=\pm 1$ with the corresponding signal received by the receiver. FIG. 3 is a diagram showing an estimator used in the apparatus for estimation and compensation of I/Q imbalance according to the embodiment of the present invention. The values of M11, M12, M21 and M22 are $\alpha_r \cos \theta_r$, $\alpha_r \sin \theta_r$, $\beta_r \sin \phi_r$ and $\beta_r \cos \phi_r$ respectively, and are sent to the receiving compensating matrix circuit 150. N is the number of the transmitted symbols. The multipliers shown in FIG. 3 may be replaced by inverters or shift registers. This simplified parameter estimation and determine estimator may apply to a communication (transmitter/receiver) system having an RF circuit without DC bias for transmitting the continuous deterministic signals.

The transmitter I/Q imbalance is estimated by transmitting two OFDM signals with $a_{k,i}=a_{-k,i}$ and $a_{k,q}=a_{-k,q}$ through the I and Q modulation path respectively so that

$$\begin{bmatrix} \hat{a}_{k,i} \\ \hat{a}_{k,q} \end{bmatrix} = \begin{bmatrix} c_i + d_i & -c_q + d_q \\ c_q + d_q & c_i - d_i \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (22)$$

$$5 \quad = \begin{bmatrix} \alpha_i \cos \theta_i & -\beta_i \sin \phi_i \\ \alpha_i \sin \theta_i & \beta_i \cos \phi_i \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (23)$$

In order to avoid the impact of receiver I/Q imbalance, only one single demodulation path (either real-part modulation path I_tx or imaginary-part modulation path Q_tx of the receiving node) is used during the estimation of transmitter I/Q imbalance. The real-part of the time-domain signal is demodulated alone using a cosine ($\cos(\omega_c t)$) carrier wave and the imaginary-part time-domain signal is demodulated alone using a sine ($\sin(\omega_c t)$) carrier wave in different time period.

15 When $a_{k,i} = a_{-k,i}$ (symmetric) and $a_{k,q} = a_{-k,q}$ (symmetric), that is both the real-part and the imaginary-part frequency domain signal are symmetric, the time-domain OFDM signal is transmitted through the Q demodulation path Q_rx and is demodulated using a cosine ($\cos(\omega_c t)$) carrier wave to demodulate the real-part time-domain signal. Then the real-part time-domain signal is converted to frequency domain by the FFT processor 500 so that

$$\begin{bmatrix} \hat{a}_{k,i} \\ \hat{a}_{k,q} \end{bmatrix} = \begin{bmatrix} c_i + d_i & -c_q + d_q \\ 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (24)$$

$$= \begin{bmatrix} \alpha_i \cos \theta_i & -\beta_i \sin \phi_i \\ 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (25)$$

If the time-domain OFDM signal is transmitted through the Q demodulation path Q_rx and is demodulated using a sine ($\sin(\omega_c t)$) carrier wave to demodulate the imaginary-part time-domain signal. Then the imaginary-part time-domain
 5 signal is converted to frequency domain by the FFT processor
 500 so that

$$\begin{bmatrix} \hat{a}_{k,i} \\ \hat{a}_{k,q} \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ c_q + d_q & c_i - d_i \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (26)$$

$$= \begin{bmatrix} 0 & 0 \\ \alpha_t \sin \theta_t & \beta_t \cos \phi_t \end{bmatrix} \cdot \begin{bmatrix} a_{k,i} \\ a_{k,q} \end{bmatrix} \dots\dots\dots (27)$$

By using the system and method disclosed above with the
 10 OFDM signals that $a_{k,i} = a_{-k,i}$ (symmetric) and $a_{k,q} = a_{-k,q}$
 (symmetric), the parameters of $\alpha_t \cos \theta_t$, $\alpha_t \sin \theta_t$, $\beta_t \sin \phi_t$ and
 $\beta_t \cos \phi_t$ can be determined respectively. Alternatively, the
 parameters for compensation of the transmitter I/Q imbalance
 may also be derived by the estimator shown in FIG. 3,
 15 wherein the values of M_{11} , M_{12} , M_{21} and M_{22} are $\alpha_t \cos \theta_t$, $-\beta_t \sin \phi_t$,
 $\alpha_t \sin \theta_t$ and $\beta_t \cos \phi_t$ respectively. These parameters
 are for use by the transmitting compensation matrix circuit
 250.

FIG. 4A and 4B respectively show constellations of an
 20 imbalanced modulation before and after the compensation.

It should be noted that the relation between the $a_{k,i}$,
 $a_{-k,i}$, $a_{k,q}$ and $a_{-k,q}$ is not necessarily limited to that
 described previously. The receiver I/Q imbalance may be
 estimated only by transmitting the signal through the same
 25 modulation path and the transmitter I/Q imbalance may be
 estimated only by receiving the signal through the same

demodulation path. However, this increases difficulty in baseband signal processing.

5 The present invention takes advantage of the modulation/demodulation characteristics of OFDM signals to estimate the receiver and transmitter I/Q imbalance, and further uses a specifically predetermined signal to simplify the estimation.

10 The foregoing description of the preferred embodiments of this invention has been presented for purposes of illustration and description. Obvious modifications or variations are possible in light of the above teaching. The embodiments were chosen and described to provide the best illustration of the principles of this invention and its practical application to thereby enable those skilled in the art to utilize the invention in various embodiments and with
15 various modifications as are suited to the particular use contemplated. All such modifications and variations are within the scope of the present invention as determined by the appended claims when interpreted in accordance with the
20 breadth to which they are fairly, legally, and equitably entitled.